

《課題》

数学 I の教科書 p23～31 の内容を、数学 I の授業用のノート（春休みの宿題の続き）に、自分なりにまとめ、例、例題、応用例題、練習を解く（ただし問は除く）。また、練習については、下の解答で答え合わせをすること。提出は5月21日（木）の登校日。

練習22 (1) $\frac{1}{3} = 0.333\cdots = 0.\dot{3}$

(2) $\frac{7}{33} = 0.2121\cdots = 0.\dot{2}\dot{1}$

(3) $\frac{55}{54} = 1.0185185\cdots = 1.0\dot{1}8\dot{5}$

(4) $-\frac{22}{7} = -3.142857142857\cdots = -3.\dot{1}428\dot{5}7$

練習23 (1) $x = 0.\dot{1}$ とおくと

(2) $x = 0.\dot{1}\dot{2}$ とおくと

$$\begin{array}{r} 10x = 1.11\cdots \\ -) \quad x = 0.11\cdots \\ \hline 9x = 1 \end{array}$$

$$\begin{array}{r} 100x = 12.1212\cdots \\ -) \quad x = 0.1212\cdots \\ \hline 99x = 12 \end{array}$$

よって $x = \frac{1}{9}$

よって $x = \frac{12}{99} = \frac{4}{33}$

(3) $x = 0.\dot{6}4\dot{8}$ とおくと

(4) $x = 6.\dot{5}4$ とおくと

$$\begin{array}{r} 1000x = 648.648648\cdots \\ -) \quad x = 0.648648\cdots \\ \hline 999x = 648 \end{array}$$

$$\begin{array}{r} 100x = 654.5454\cdots \\ -) \quad x = 6.5454\cdots \\ \hline 99x = 648 \end{array}$$

よって $x = \frac{648}{999} = \frac{24}{37}$

よって $x = \frac{648}{99} = \frac{72}{11}$

練習24

数の範囲	加法	減法	乗法	除法
自然数	○	×	○	×
整数	○	○	○	×
有理数	○	○	○	○
実数	○	○	○	○

練習25 (1) $\left| -\frac{3}{4} \right| = -\left(-\frac{3}{4} \right) = \frac{3}{4}$

(2) $|-5+3| = |-2| = -(-2) = 2$

(3) $|-5|+|3| = -(-5)+3 = 8$

(4) $3-\pi < 0$ であるから $|3-\pi| = -(3-\pi) = \pi-3$

練習26 (1) $AB = |4-2| = |2| = 2$

(2) $AB = |6-(-1)| = |7| = 7$

(3) $AB = |-7-(-3)| = |-4| = 4$

練習27 (1) ± 7 (2) $\sqrt{25} = 5$

練習28 $(\sqrt{7})^2 = 7$, $(-\sqrt{15})^2 = 15$

練習29 (1) $4\sqrt{3} + 5\sqrt{3} - 7\sqrt{3} = (4 + 5 - 7)\sqrt{3} = 2\sqrt{3}$

(2) $3\sqrt{50} - 4\sqrt{18} + \sqrt{32} = 15\sqrt{2} - 12\sqrt{2} + 4\sqrt{2} = (15 - 12 + 4)\sqrt{2} = 7\sqrt{2}$

(3) $(\sqrt{7} + 2)(\sqrt{7} - 2) = (\sqrt{7})^2 - 2^2 = 7 - 4 = 3$

(4) $(4\sqrt{2} - 3\sqrt{3})(5\sqrt{2} + 2\sqrt{3}) = 4\sqrt{2} \cdot 5\sqrt{2} + 4\sqrt{2} \cdot 2\sqrt{3} - 3\sqrt{3} \cdot 5\sqrt{2} - 3\sqrt{3} \cdot 2\sqrt{3}$
 $= 40 + 8\sqrt{6} - 15\sqrt{6} - 18 = 22 - 7\sqrt{6}$

(5) $(\sqrt{3} + 2\sqrt{6})^2 = (\sqrt{3})^2 + 2 \cdot \sqrt{3} \cdot 2\sqrt{6} + (2\sqrt{6})^2$
 $= 3 + 12\sqrt{2} + 24 = 27 + 12\sqrt{2}$

(6) $(3\sqrt{2} - 2\sqrt{7})^2 = (3\sqrt{2})^2 - 2 \cdot 3\sqrt{2} \cdot 2\sqrt{7} + (2\sqrt{7})^2$
 $= 18 - 12\sqrt{14} + 28 = 46 - 12\sqrt{14}$

練習30 (1) $\frac{18}{\sqrt{6}} = \frac{18 \times \sqrt{6}}{\sqrt{6} \times \sqrt{6}} = \frac{18\sqrt{6}}{6} = 3\sqrt{6}$

(2) $\frac{\sqrt{3}}{2 + \sqrt{3}} = \frac{\sqrt{3}(2 - \sqrt{3})}{(2 + \sqrt{3})(2 - \sqrt{3})} = \frac{2\sqrt{3} - (\sqrt{3})^2}{2^2 - (\sqrt{3})^2} = 2\sqrt{3} - 3$

(3) $\frac{\sqrt{5} + \sqrt{2}}{\sqrt{5} - \sqrt{2}} = \frac{(\sqrt{5} + \sqrt{2})^2}{(\sqrt{5} - \sqrt{2})(\sqrt{5} + \sqrt{2})} = \frac{5 + 2\sqrt{10} + 2}{(\sqrt{5})^2 - (\sqrt{2})^2} = \frac{7 + 2\sqrt{10}}{3}$

(4) $\frac{3\sqrt{7} - \sqrt{3}}{\sqrt{7} + \sqrt{3}} = \frac{(3\sqrt{7} - \sqrt{3})(\sqrt{7} - \sqrt{3})}{(\sqrt{7} + \sqrt{3})(\sqrt{7} - \sqrt{3})} = \frac{21 - 3\sqrt{21} - \sqrt{21} + 3}{(\sqrt{7})^2 - (\sqrt{3})^2}$
 $= \frac{24 - 4\sqrt{21}}{4} = 6 - \sqrt{21}$

練習31 (1) $x = \frac{1}{\sqrt{7} + \sqrt{5}} = \frac{\sqrt{7} - \sqrt{5}}{(\sqrt{7} + \sqrt{5})(\sqrt{7} - \sqrt{5})} = \frac{\sqrt{7} - \sqrt{5}}{2}$

$y = \frac{1}{\sqrt{7} - \sqrt{5}} = \frac{\sqrt{7} + \sqrt{5}}{(\sqrt{7} - \sqrt{5})(\sqrt{7} + \sqrt{5})} = \frac{\sqrt{7} + \sqrt{5}}{2}$

よって $x + y = \frac{\sqrt{7} - \sqrt{5}}{2} + \frac{\sqrt{7} + \sqrt{5}}{2} = \sqrt{7}$

別解 $x + y = \frac{1}{\sqrt{7} + \sqrt{5}} + \frac{1}{\sqrt{7} - \sqrt{5}} = \frac{(\sqrt{7} - \sqrt{5}) + (\sqrt{7} + \sqrt{5})}{(\sqrt{7} + \sqrt{5})(\sqrt{7} - \sqrt{5})} = \frac{2\sqrt{7}}{2} = \sqrt{7}$

(2) $xy = \frac{1}{\sqrt{7} + \sqrt{5}} \cdot \frac{1}{\sqrt{7} - \sqrt{5}} = \frac{1}{2}$

(3) $x^2 + y^2 = (x + y)^2 - 2xy = (\sqrt{7})^2 - 2 \cdot \frac{1}{2} = 6$

(4) $x^2y + xy^2 = xy(x + y) = \frac{1}{2} \cdot \sqrt{7} = \frac{\sqrt{7}}{2}$

練習1 **応用例題** 1)、(2)より $x + y = \sqrt{5}$ 、 $xy = 1$

よって $x^3 + y^3 = (x + y)^3 - 3xy(x + y) = (\sqrt{5})^3 - 3 \cdot 1 \cdot \sqrt{5} = 2\sqrt{5}$